

# Number of people who drowned by falling into a pool correlates with Films Nicolas Cage appeared in



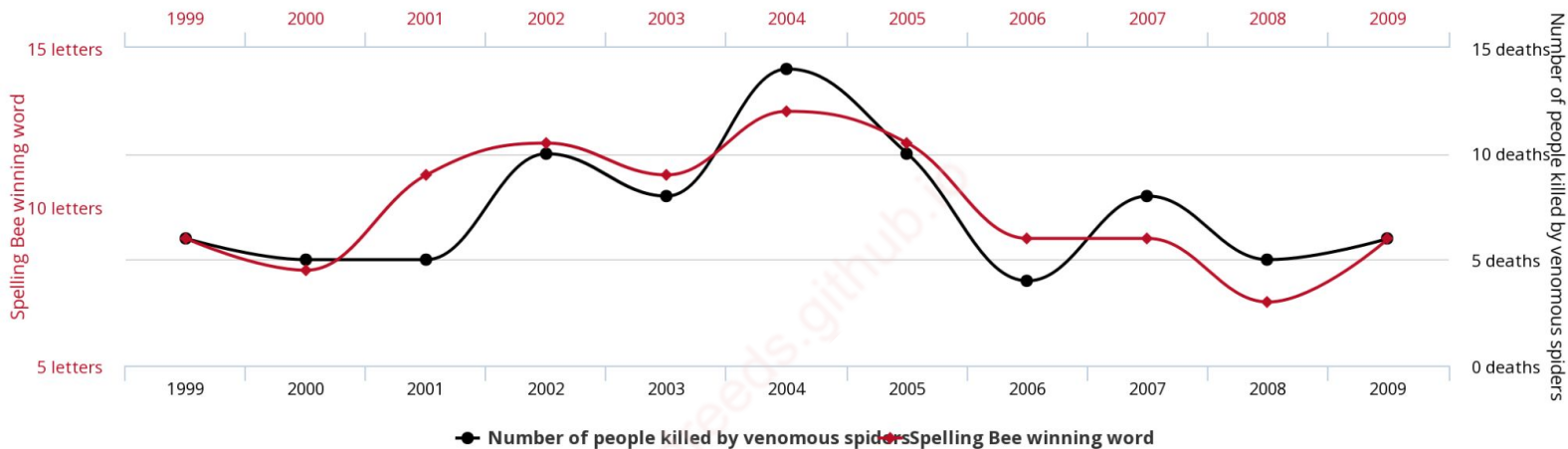
tylervigen.com



# Letters in Winning Word of Scripps National Spelling Bee

correlates with

## Number of people killed by venomous spiders



tylervigen.com



Correlation



Causality

# CAUSALITY

## PART I - CONFOUNDING

André dos Santos, *Ph.D.*



**Have you ever  
noticed that,  
among the people  
you date**

**the  
attractive  
ones tend to  
be jerks?**



# The Monty Hall problem

"Let's make a deal"



# The Monty Hall problem

"Let's make a deal"



# The Monty Hall problem

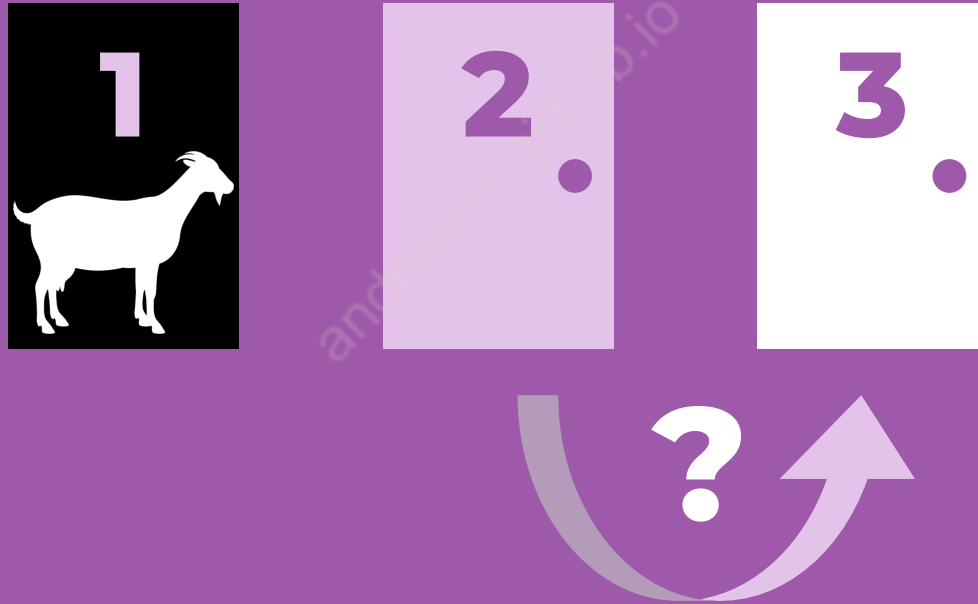
"Let's make a deal"





# The Monty Hall problem

"Let's make a deal"



# The Ladder of Causation



**SEEING**

ASSOCIATION



**DOING**

INTERVENTION



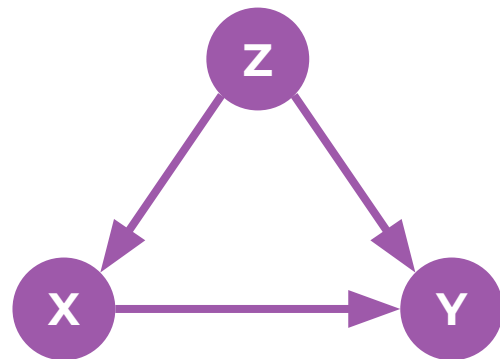
**IMAGINING**

COUNTERFACTUALS

# Confounding

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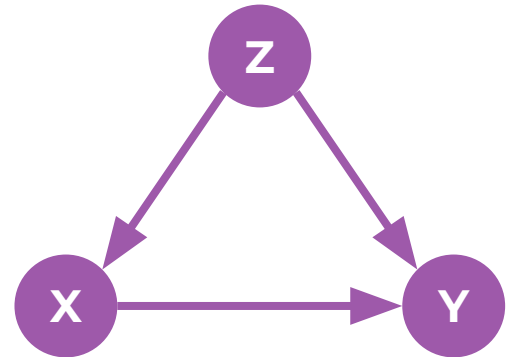
- Not a statistical notion
- $P(Y|X) \neq P(Y|\text{do}(X))$
- **Discrepancy** between what we want to assess (the causal effect) and what we actually do assess using statistical method



**Backdoor path** is any path from X to Y that starts with an arrow pointing into X.

**X ← Z → Y**

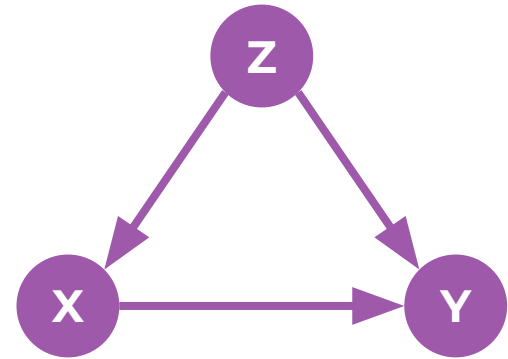
X and Y will be **deconfounded** if we block every backdoor path.



**Backdoor path** is any path from X to Y that starts with an arrow pointing into X.

**X ← Z → Y**

X and Y will be **deconfounded** if we block every backdoor path.



# Flow of Information In Causal Graph



**CHAIN**

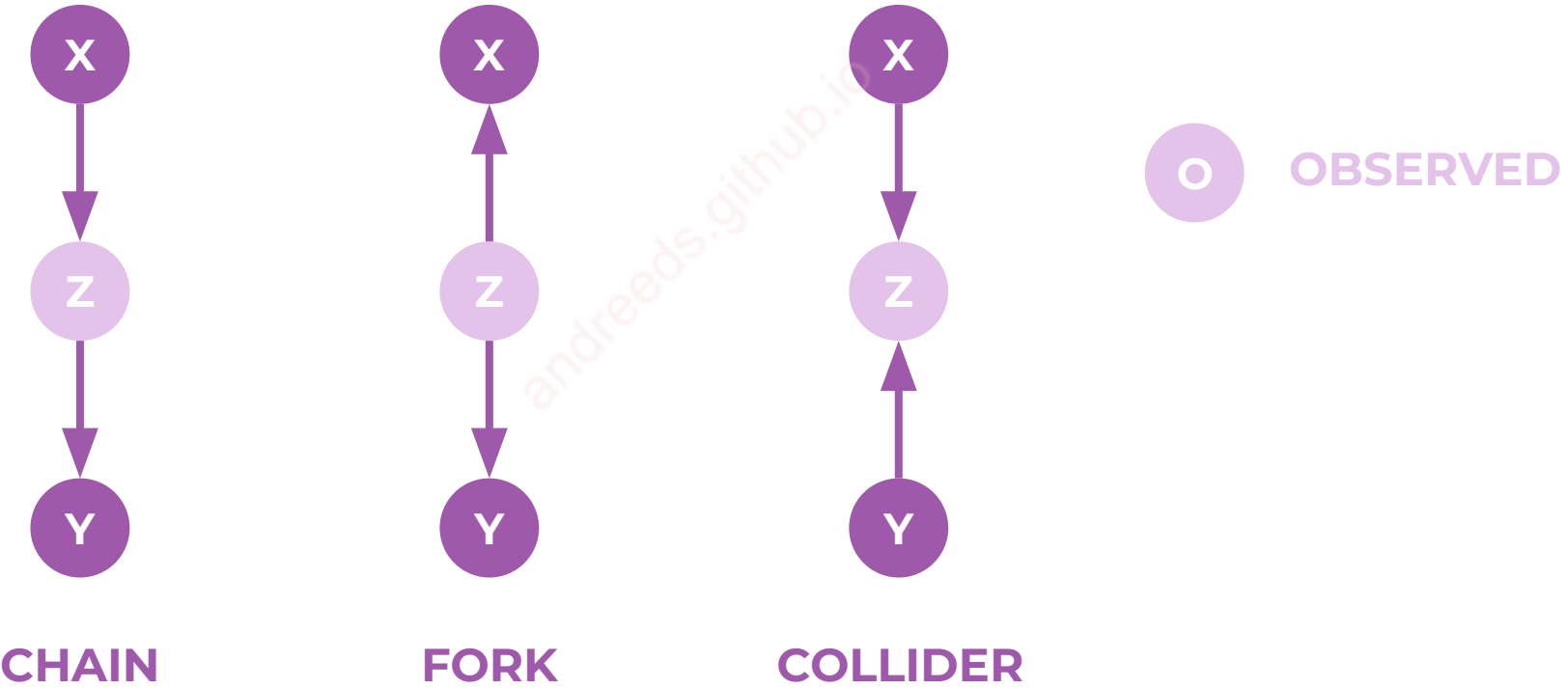


**FORK**

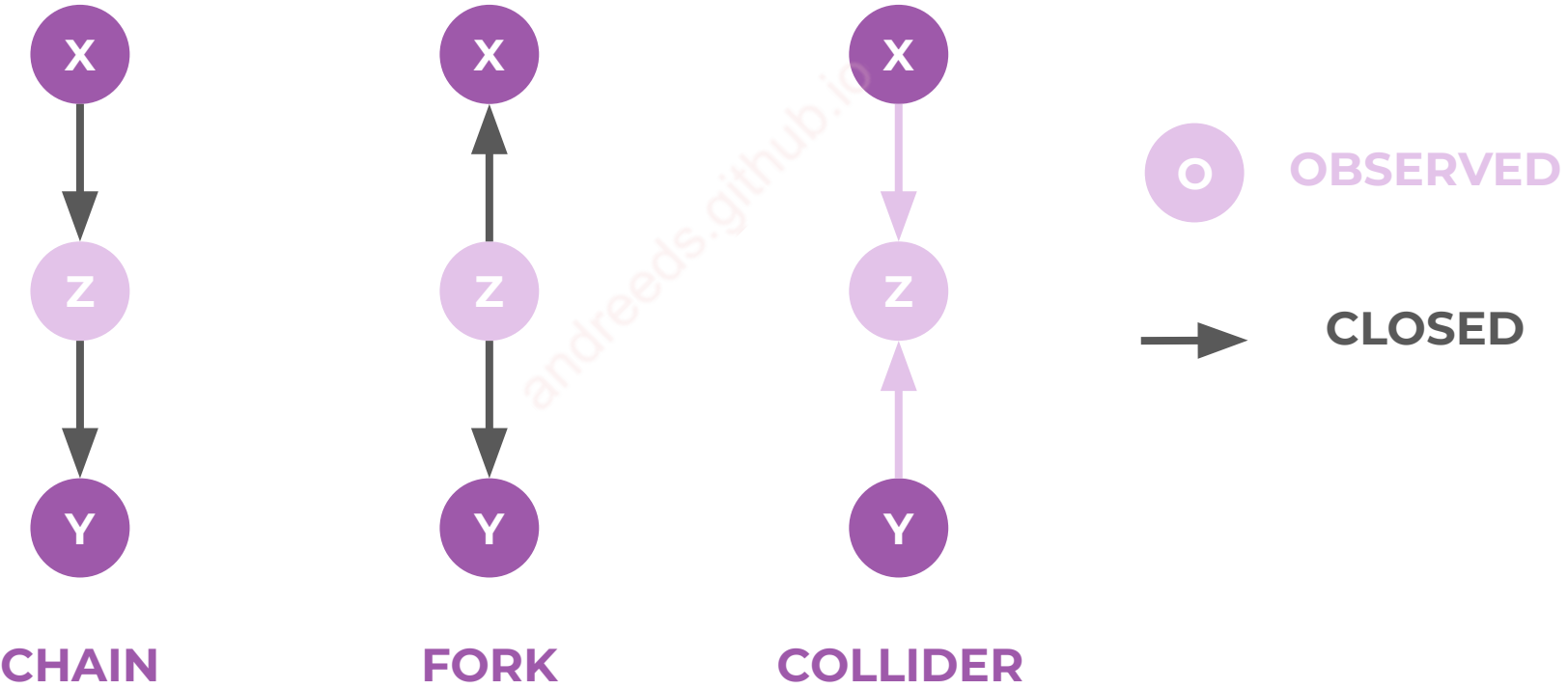


**COLLIDER**

# Flow of Information In Causal Graph

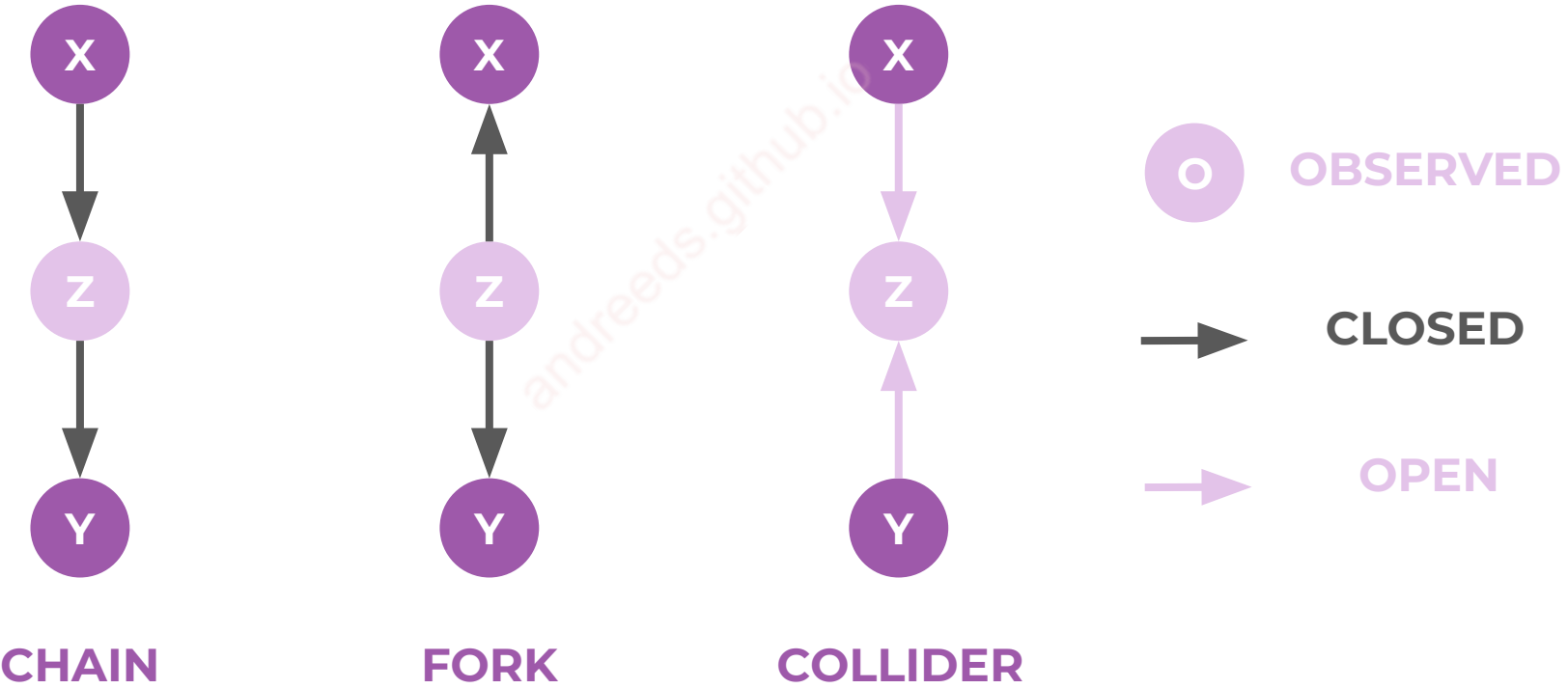


# Flow of Information In Causal Graph

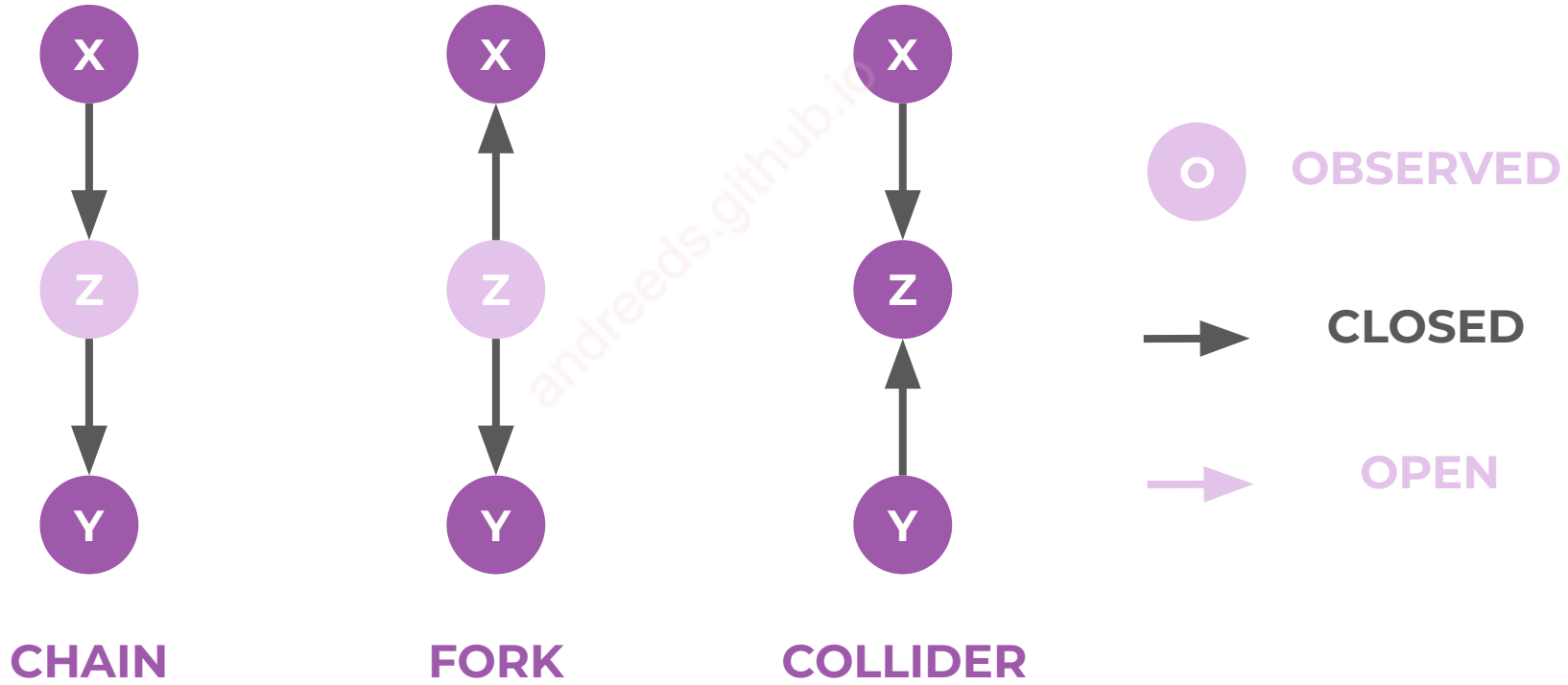




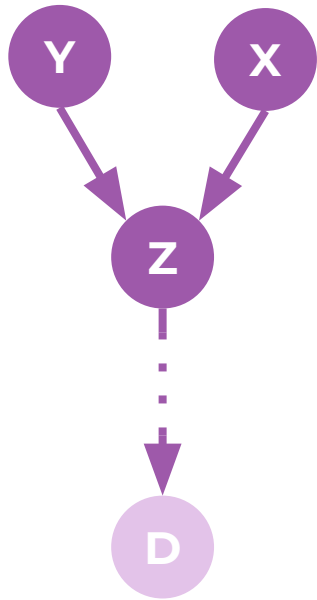
# Flow of Information In Causal Graph



# Flow of Information In Causal Graph



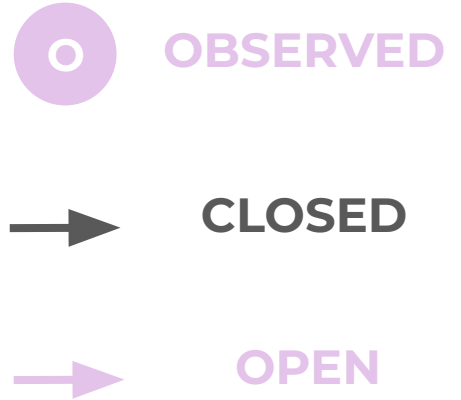
# Flow of Information In Causal Graph



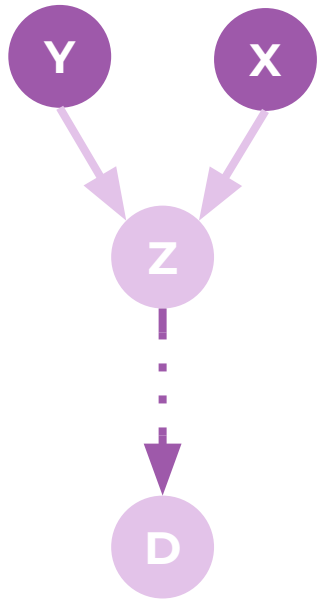
**\*DESCENDENTS**



**COLLIDER**



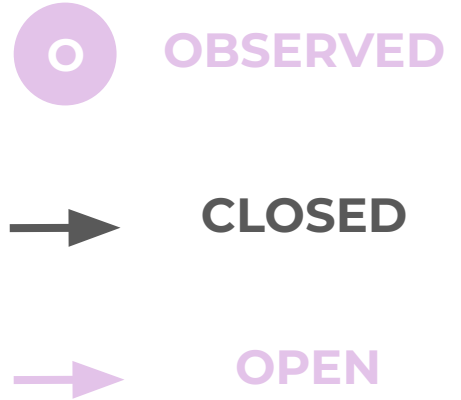
# Flow of Information In Causal Graph



**\*DESCENDENTS**



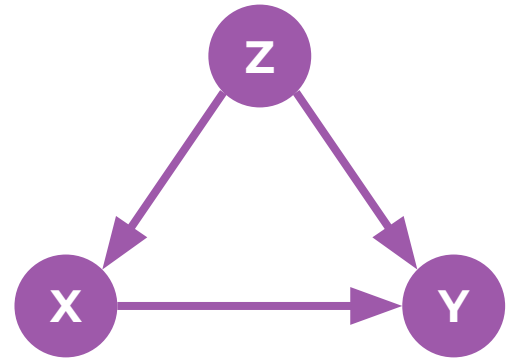
**COLLIDER**

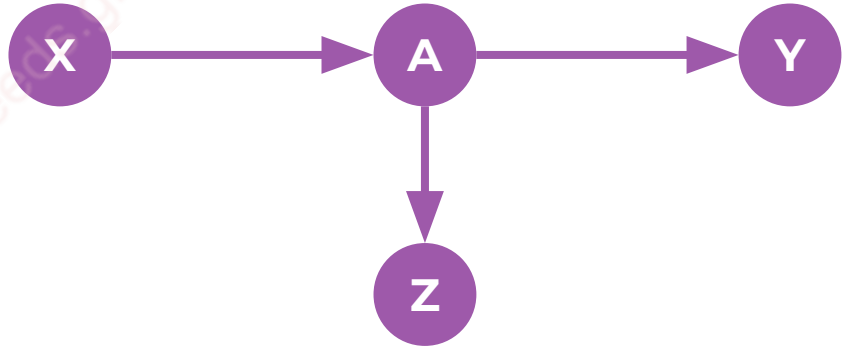


**Backdoor path** is any path from X to Y that starts with an arrow pointing into X.



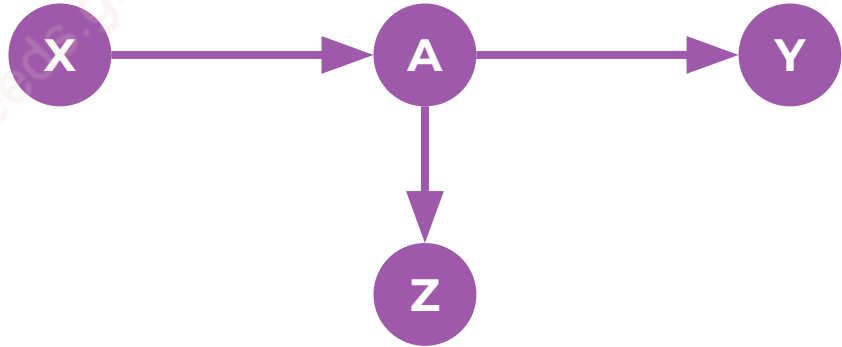
X and Y will be **deconfounded** if we block every backdoor path.

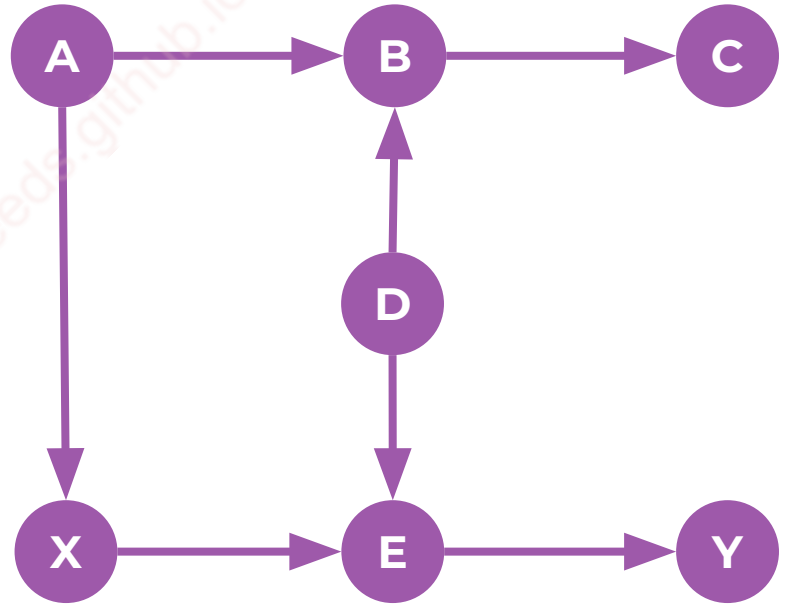






- No backdoor

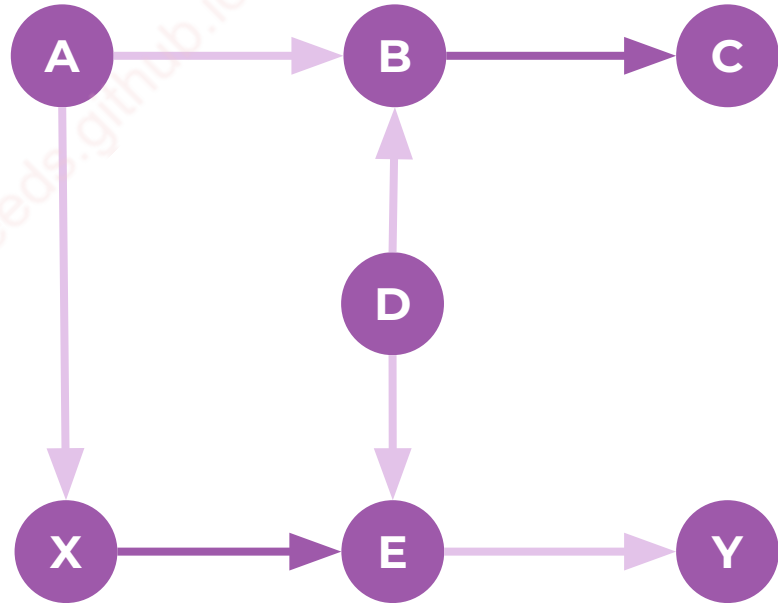






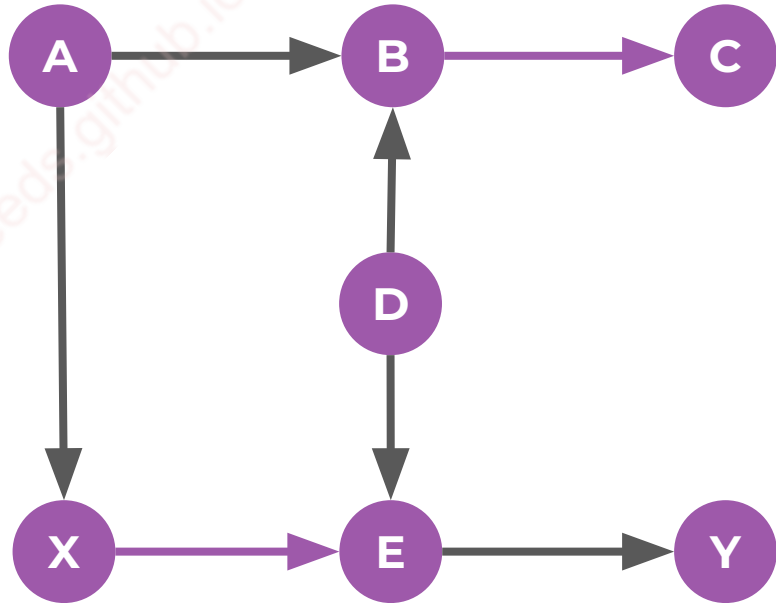


- One backdoor path
- $X \leftarrow A \rightarrow B \leftarrow D \rightarrow E \rightarrow Y$



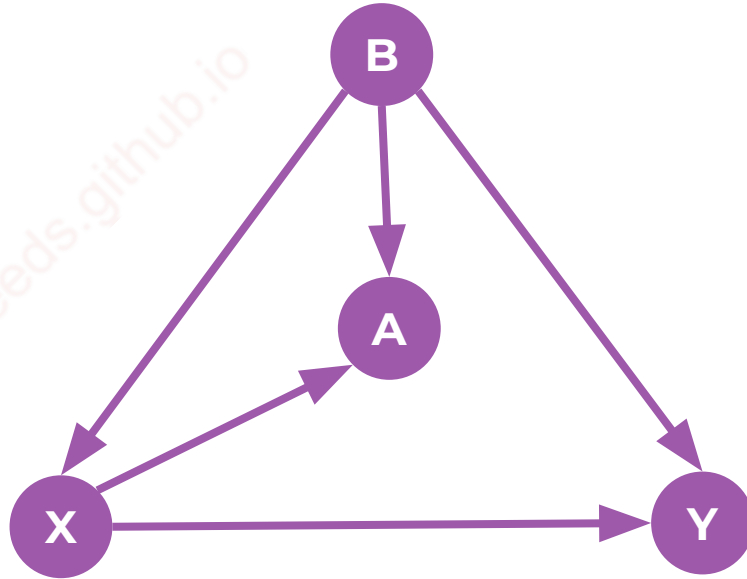


- One backdoor path
- $X \leftarrow A \rightarrow B \leftarrow D \rightarrow E \rightarrow Y$
- Control  $\emptyset$



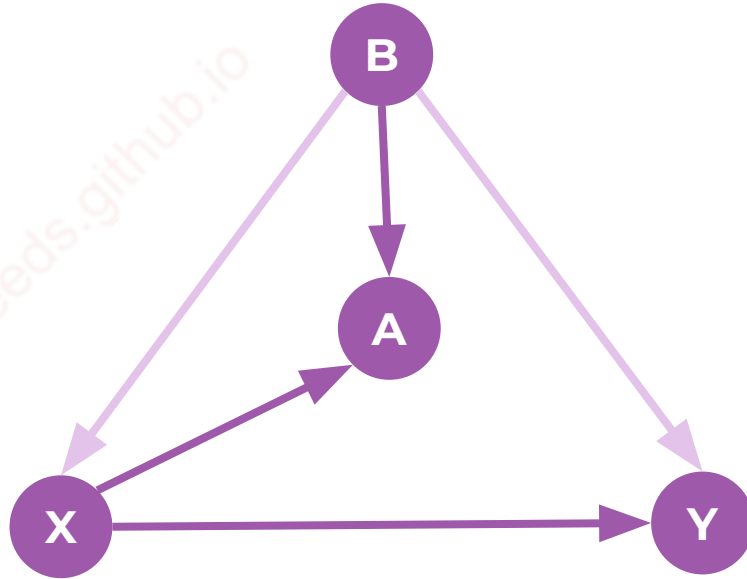


- One backdoor path
- $X \leftarrow B \rightarrow Y$



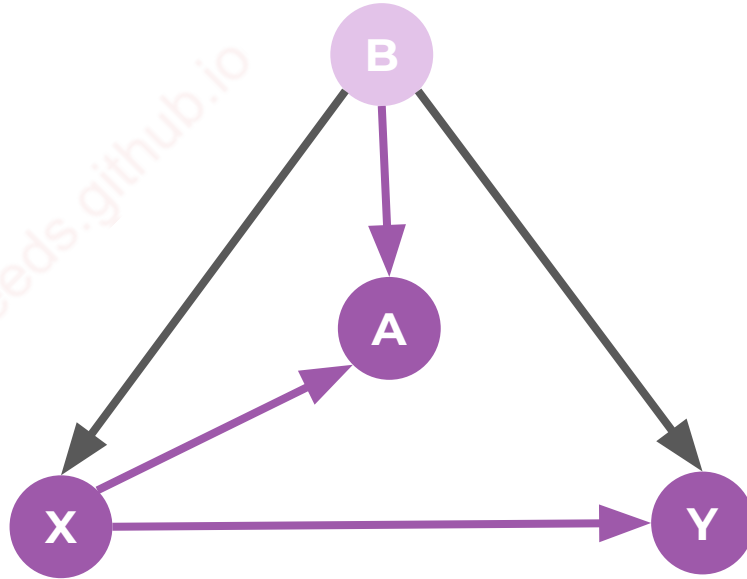


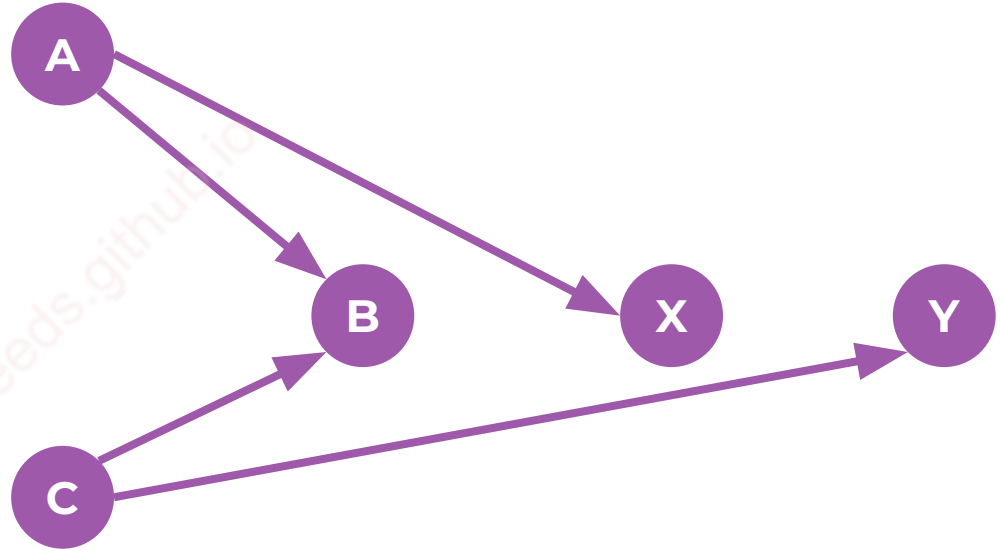
- One backdoor path
- $X \leftarrow B \rightarrow Y$

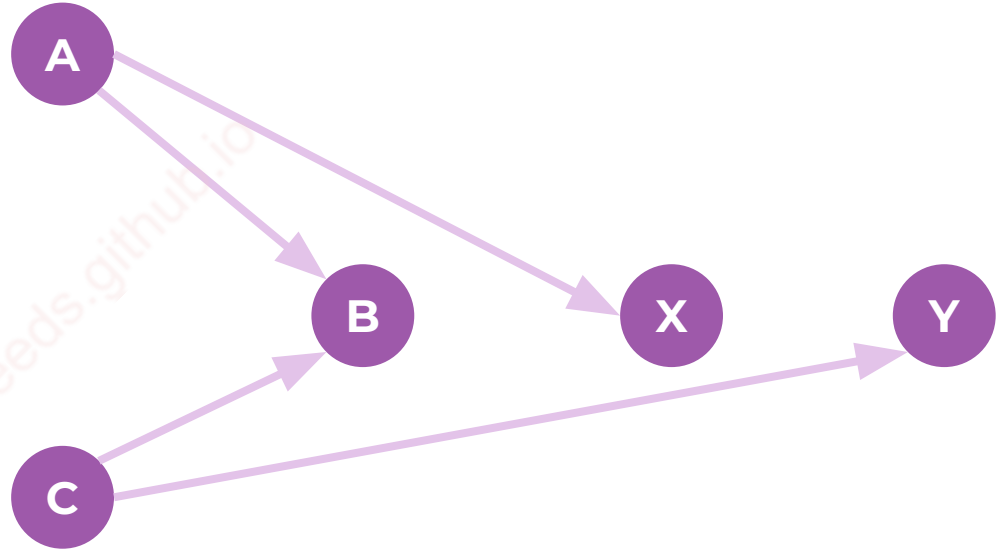




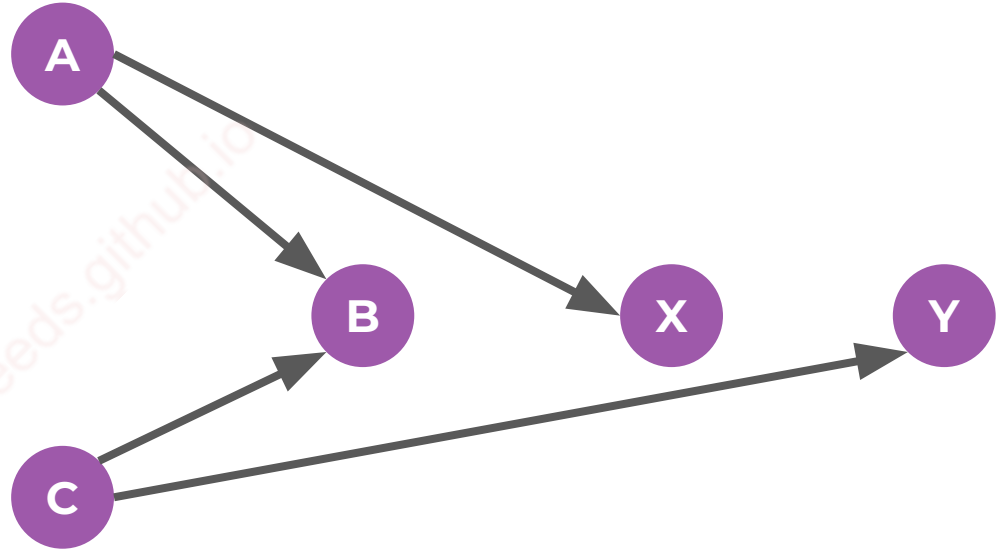
- One backdoor path
- $X \leftarrow B \rightarrow Y$
- Control B





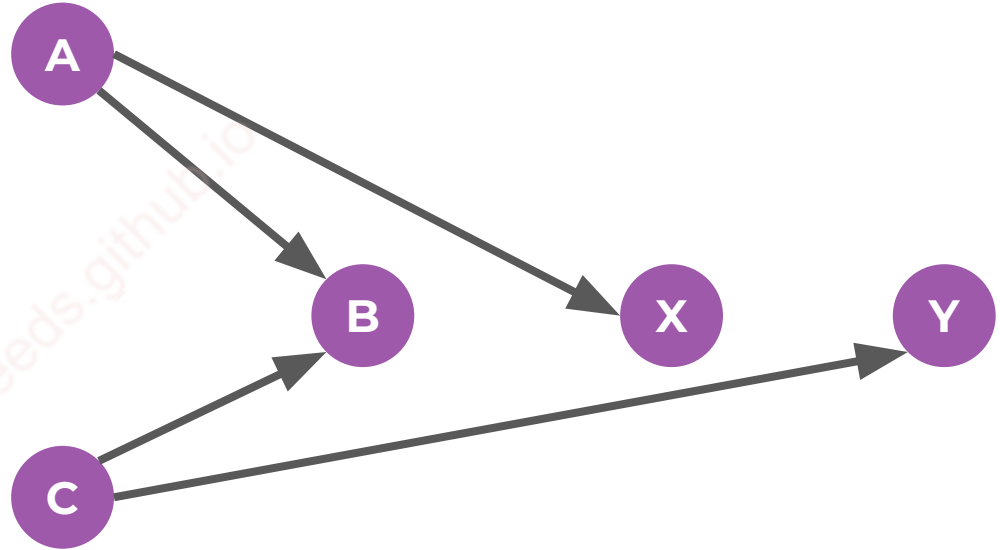


- One backdoor path
  - $X \leftarrow A \rightarrow B \leftarrow C \rightarrow Y$



- One backdoor path
  - $X \leftarrow A \rightarrow B \leftarrow C \rightarrow Y$
- Control  $\emptyset$

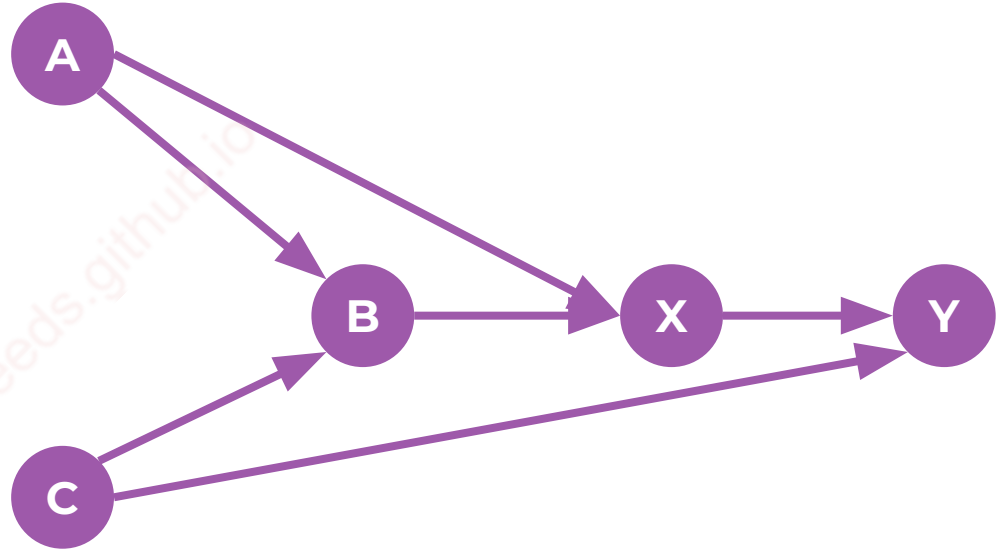


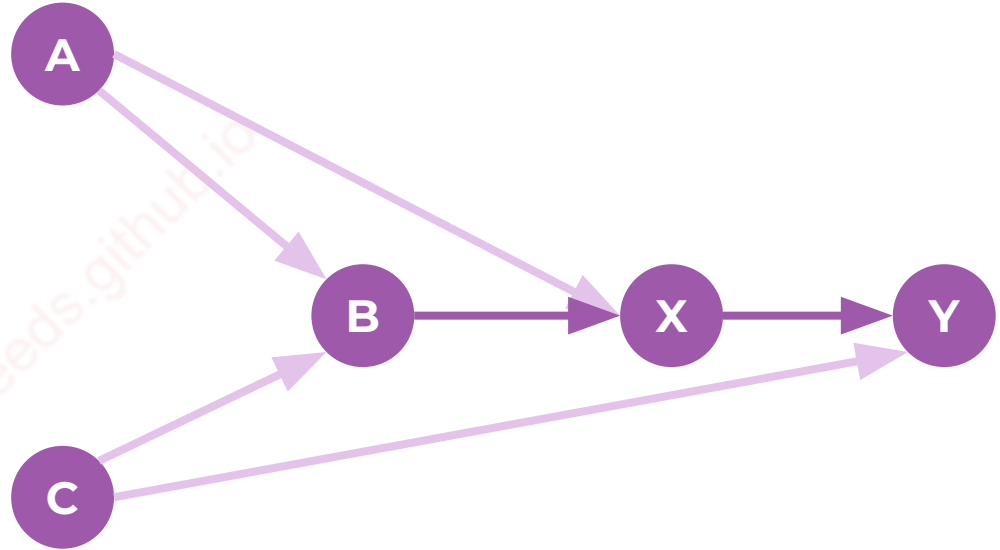


- One backdoor path
  - $X \leftarrow A \rightarrow B \leftarrow C \rightarrow Y$
- Control  $\emptyset$

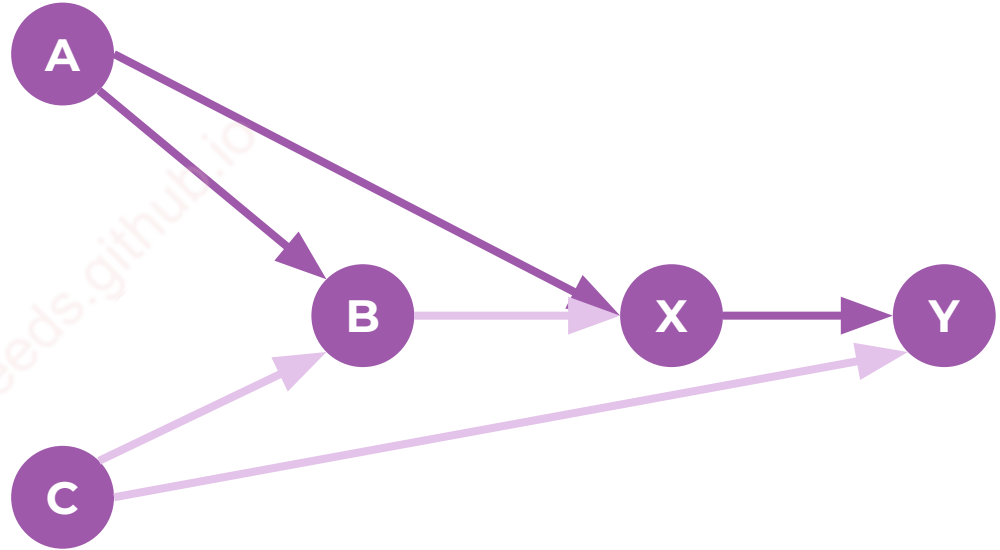
A := Societal norms  
B := Seat belt usage  
C := Safety and health related measures

X := Smoking  
Y := Lung disease

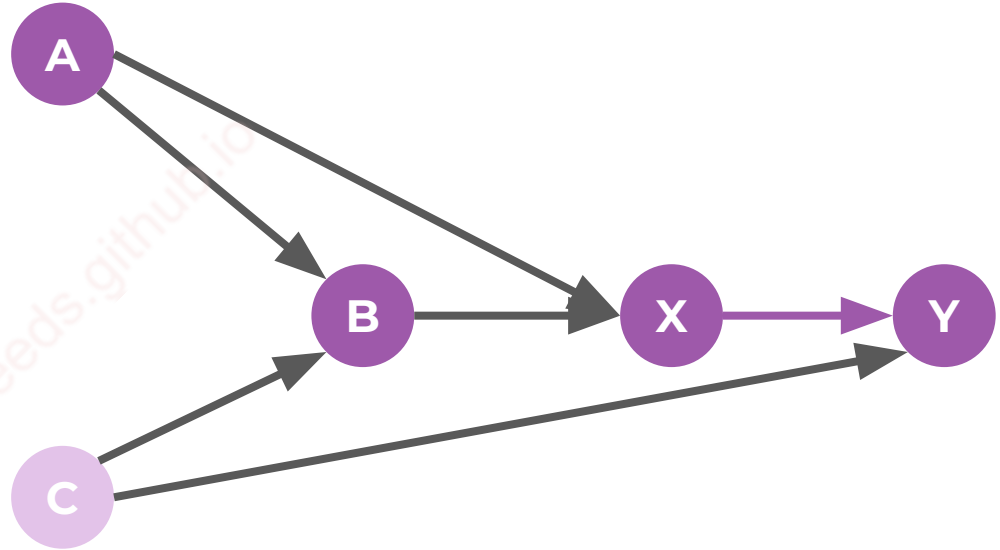




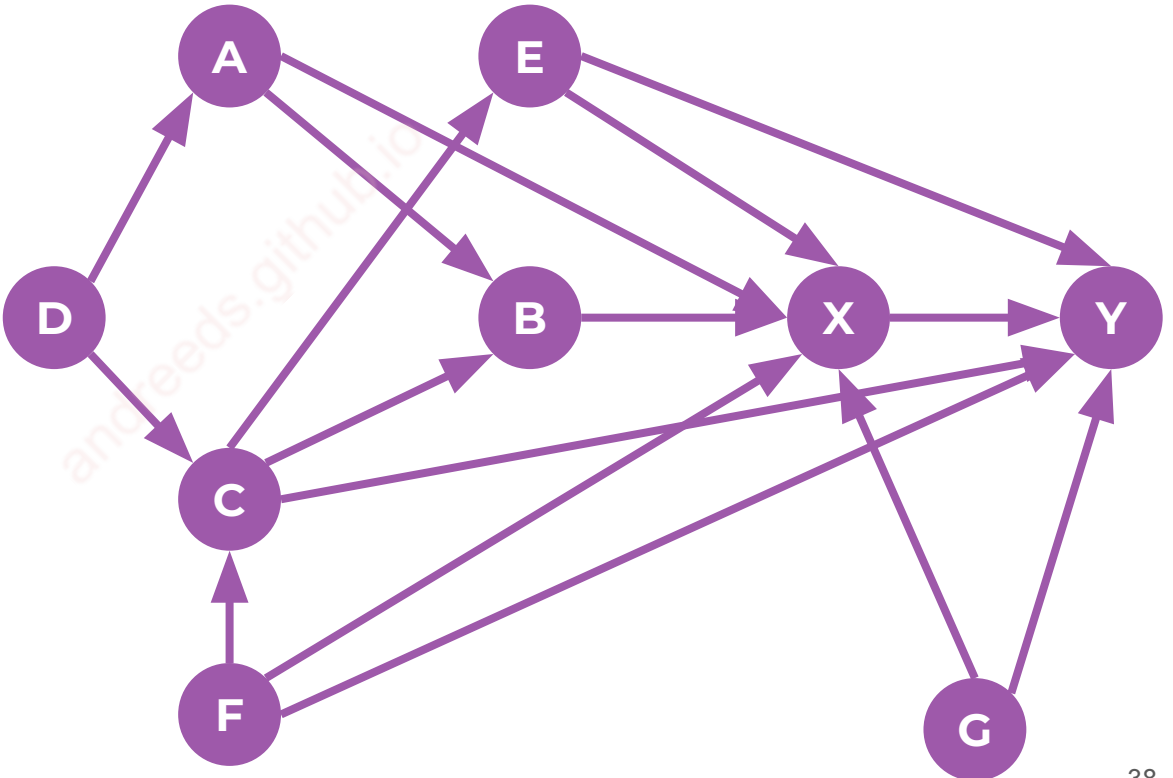
- Two backdoor paths
  - $X \leftarrow A \rightarrow B \leftarrow C \rightarrow Y$



- Two backdoor paths
  - $X \leftarrow A \rightarrow B \leftarrow C \rightarrow Y$
  - $X \leftarrow B \leftarrow C \rightarrow Y$



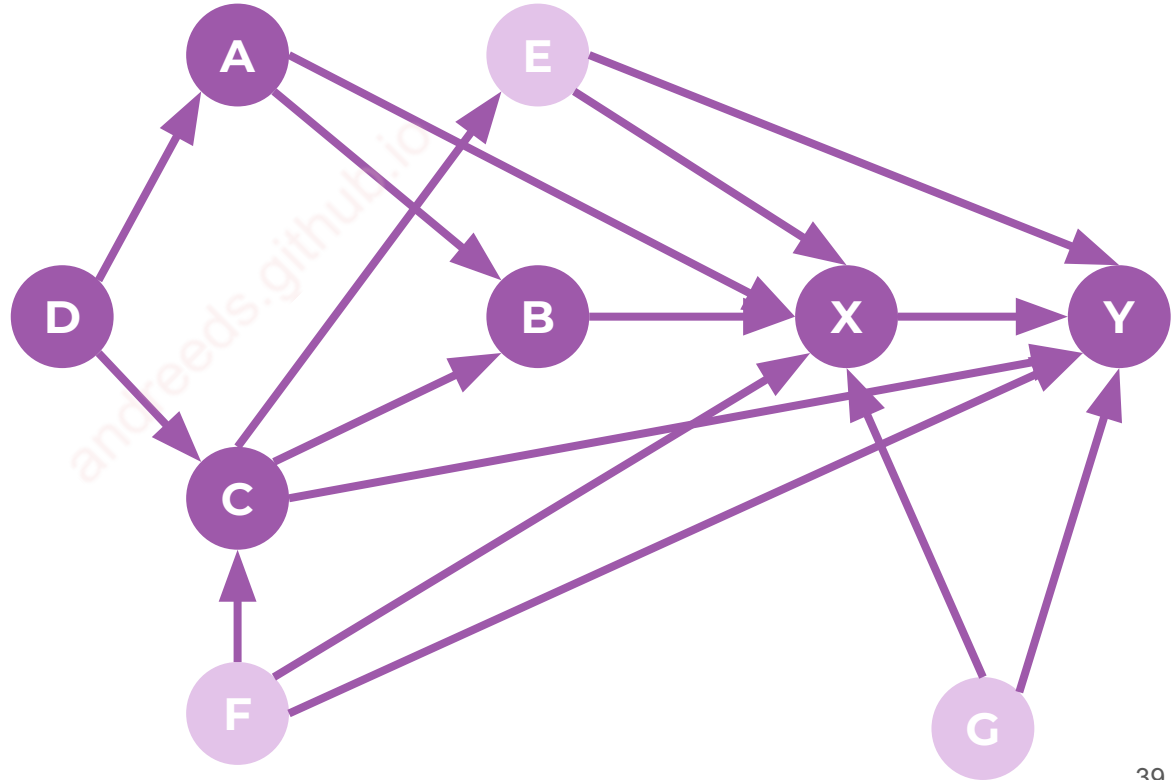
- Two backdoor paths
  - $X \leftarrow A \rightarrow B \leftarrow C \rightarrow Y$
  - $X \leftarrow B \leftarrow C \rightarrow Y$
- Control C



A := Societal norms  
B := Seat belt usage  
C := Safety and health related measures  
D := Parental asthma  
E := Chronic bronchitis  
F := Sex  
G := Socioeconomic status  
X := Smoking  
Y := Lung disease



- Control E, F, and G



A := Societal norms  
B := Seat belt usage  
C := Safety and health related measures  
D := Parental asthma  
E := Chronic bronchitis  
F := Sex  
G := Socioeconomic status  
X := Smoking  
Y := Lung disease

# The Monty Hall problem










"Let's make a deal"





# The Monty Hall problem

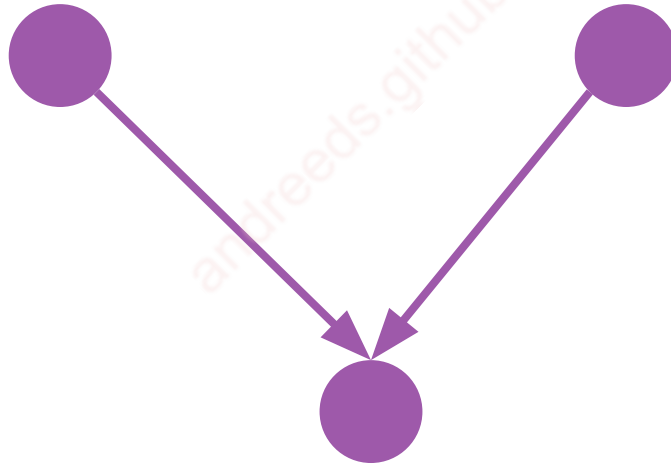
Chosen

Door 1	Door 2	Door 3	Outcome if switch	Outcome if stay
			Lose	Win
			Win	Lose
			Win	Lose

# The Monty Hall problem

Your Door

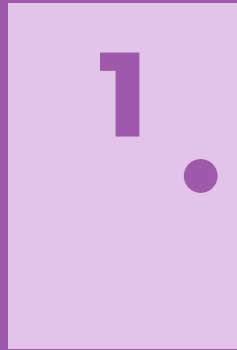
Location of Car



Second Door Opened







# The Monty Hall problem 2.0

"Let's **fake** a deal"









# The Monty Hall problem 2.0

"Let's **fake** a deal"

Door You Choose	Door with Car	Door Opened	Outcome if switch	Outcome if stay
1	1	2 	Lose	<b>Win</b>
1	1	3 	Lose	<b>Win</b>
1	2	2 	Lose	Lose
1	2	3 	<b>Win</b>	Lose
1	3	2 	<b>Win</b>	Lose
1	3	3 	Lose	Lose







# The Monty Hall problem 2.0

"Let's **fake** a deal"

Door You Choose	Door with Car	Door Opened	Outcome if switch	Outcome if stay
1	1	2 	Lose	<b>Win</b>
1	1	3 	Lose	<b>Win</b>
1	2	2 	Lose	Lose
1	2	3 	<b>Win</b>	Lose
1	3	2 	<b>Win</b>	Lose
1	3	3 	Lose	Lose

# The Monty Hall problem 2.0

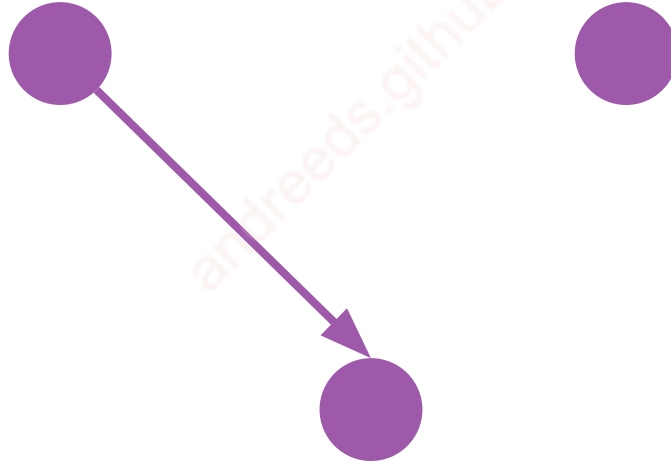
"Let's **fake** a deal"

Door You Choose	Door with Car	Door Opened	Outcome if switch	Outcome if stay
1	1	2 	Lose	<b>Win</b>
1	1	3 	Lose	<b>Win</b>
1	2	2 	Lose	Lose
1	2	3 	<b>Win</b>	Lose
1	3	2 	<b>Win</b>	Lose
1	3	3 	Lose	Lose

# The Monty Hall problem

Your Door

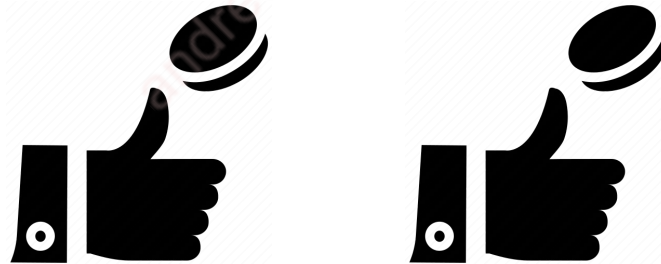
Location of Car



Second Door Opened

# 2 coins and 1 date

Berkson's Paradox



Write down the results only when **at least** one of them comes up **heads**



# 2 coins and 1 date

Berkson's Paradox

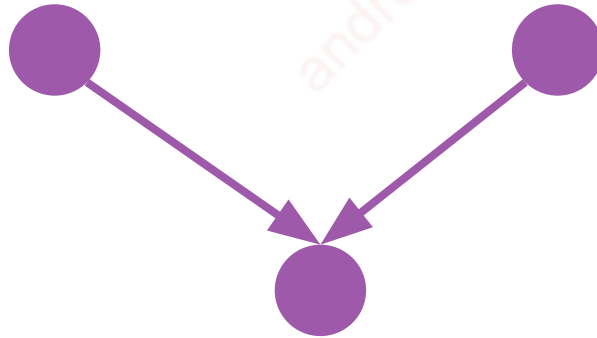
Coin 1	Coin 2	$\Omega$
Heads	Heads	25
Heads	<b>Tails</b>	<b>23</b>
<b>Tails</b>	Heads	27

# 2 coins and 1 date

Berkson's Paradox

First coin toss

Second coin toss



Registered Event

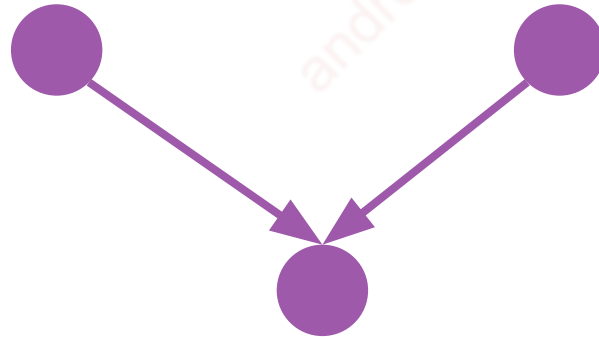
Coin 1	Coin 2	$\Omega$
Heads	Heads	25
Heads	<b>Tails</b>	<b>23</b>
<b>Tails</b>	Heads	27
Tails	Tails	X

# 2 coins and 1 date

"How Not to Be Wrong" by Jordan Ellenberg

Attractiveness

Nice Personality



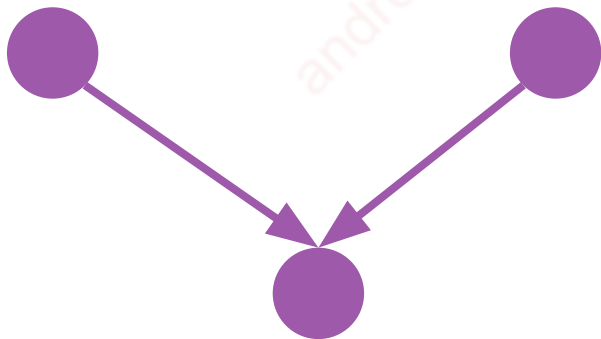
Dating Material

# 2 coins and 1 date

"How Not to Be Wrong" by Jordan Ellenberg

Attractiveness

Nice Personality



Dating Material

Nice



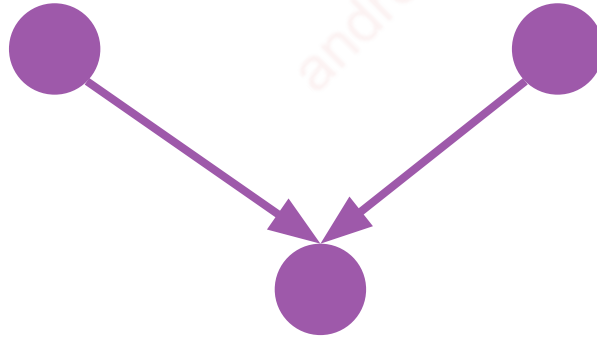
Attractive

# 2 coins and 1 date

"How Not to Be Wrong" by Jordan Ellenberg

Attractiveness

Nice Personality



Dating Material

Nice



Attractive

# CAUSALITY

## PART I - CONFOUNDING

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